



Deep Learning for Computer Vision

Dr. Konda Reddy Mopuri
Mehta Family School of Data Science and Artificial Intelligence
IIT Guwahati
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So far in the class..



- Recap of ML, Artificial neuron, MLP

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- CNNs: building blocks and architecture evolution

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- Recap of ML, Artificial neuron, MLP
- CNNs: building blocks and architecture evolution
- Training DNNs-I: Nonlinearity, weight initialization, regularization
- Today: Training DNNs-II (Optimizer: update rules, learning rate, early stopping, post-training, etc.)



Different update rules for SGD

Issues with SGD



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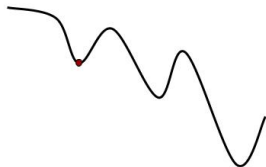
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 - May have local minima
 - May have saddle points



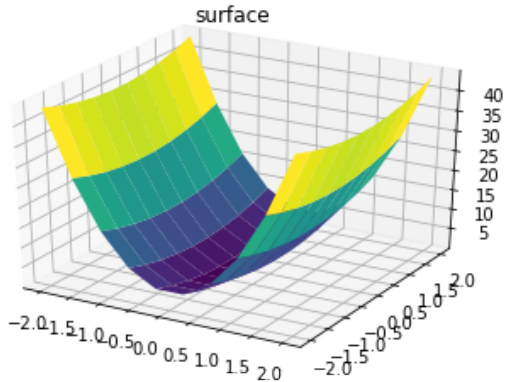
Stuck at a local minimum



Stuck at a saddle point

Issues with SGD

- DNNs are trained via SGD: $w_{t+1} = w_t - \eta \cdot \nabla_w J(w)$
- Loss is a high dimensional function
 - May vary swiftly in direction and slowly in the other



Issues with SGD

- SGD leads to jitter along the deep dimension and slow progress along the shallow one

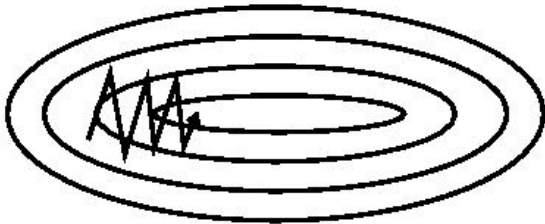


Figure credits: [Sebastian Ruder](#)

SGD+Momentum



SGD+Momentum

SGD

$$w_{t+1} = w_t - \eta \cdot \nabla_w J(w)$$

$$v_0 = 0$$

$$v_{t+1} = \rho \cdot v_t + \nabla_w J(w)$$

$$w_{t+1} = w_t - \eta \cdot v_{t+1}$$

I Sutskever et al., ICML 2013

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- Aggregates velocity: exponential moving average over gradients
- ρ is the friction (typically set to 0.9 or 0.99)

I Sutskever et al., ICML 2013

SGD+Momentum



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SGD

$$w_{t+1} = w_t - \eta \cdot \nabla_w J(w)$$

```
for i in range(num_iters):  
→ dw = grad(J, W, x, y)  
→ w- = η · dw
```

$$v_0 = 0$$

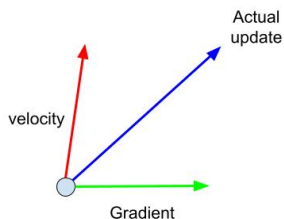
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$$w_{t+1} = w_t - \eta \cdot v_{t+1}$$

```
v_0 = 0  
for i in range(num_iters):  
→ dw = grad(J, W, x, y)  
→ v = ρ · v + dw  
→ w- = η · v
```

I Sutskever et al., ICML 2013

SGD+Momentum

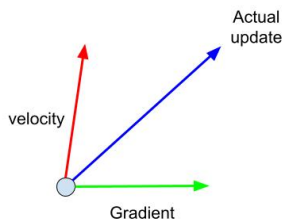


Momentum Update

① How can momentum help?

I Sutskever et al., ICML 2013

SGD+Momentum

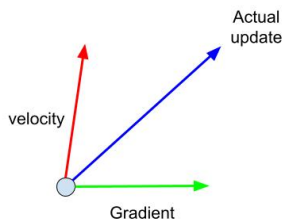


Momentum Update

- ① How can momentum help?
 - Optimization proceeds even at the local minimum or saddle point (because of the accumulated velocity)

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SGD+Momentum



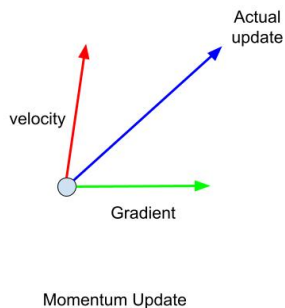
Momentum Update

① How can momentum help?

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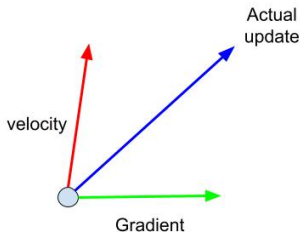
① How can momentum help?

- Optimization proceeds even at the local minimum or saddle point (because of the accumulated velocity)
- Jitter is reduced in ravine like loss surfaces
- Updates are more smoothed out (less noisy because of the exponential averaging)

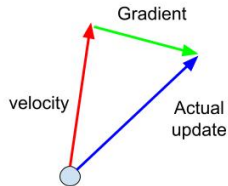
I Sutskever et al., ICML 2013

Nesterov Momentum

- ① Look ahead with the velocity, then take a step in the gradient's direction



Momentum Update



Nesterov Momentum

I Sutskever et al., ICML 2013



Nesterov Momentum

$$v_0 = 0$$

for i in range(num_iters):

$$\rightarrow dw = \text{grad}(J, W + \rho \cdot v, x, y)$$

$$\rightarrow v = \rho \cdot v + dw$$

$$\rightarrow w^- = \eta \cdot v$$

I Sutskever et al., ICML 2013



- ① Adaptive (or, per-parameter) learning rates are introduced

Duchi et al. 2011, JMLR

Ada Grad



- ① Adaptive (or, per-parameter) learning rates are introduced
- ② Parameter-wise scaling of the learning rate by the aggregated gradient

Duchi et al. 2011, JMLR

Ada Grad



```
grad_sq = 0
for i in range(max_iters):
    → dw = →grad(J,w,x,y)
    →grad_sq += dw
    → w = w - η · dw / (sqrt(grad_sq) + ε)
```

- Optimization progress along the steep directions is attenuated

Duchi et al. 2011, JMLR

Ada Grad



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grad_sq = 0
for i in range(max_iters):
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- Optimization progress along the steep directions is attenuated
- Along the flat directions is accelerated

Duchi et al. 2011, JMLR

RMS Prop



- ① If Ada Grad is run for too long
 - the gradients accumulate to a big value
 - \rightarrow update becomes too small (or, learning rate is reduced continuously)

RMS Prop



- ① If Ada Grad is run for too long
 - the gradients accumulate to a big value
 - \rightarrow update becomes too small (or, learning rate is reduced continuously)
- ② RMS prop (a leaky version of Ada Grad) addresses this using a friction coefficient (ρ)

RMS Prop



```
grad_sq = 0
for i in range(max_iters):
    → dw = →grad(J,w,x,y)
    →grad_sq =  $\rho \cdot \text{grad\_sq} + (1 - \rho) \cdot dw$ 
    →  $w- = \eta \cdot dw / (\text{sqrt}(\text{grad\_sq}) + \epsilon)$ 
```

Adam



- ① Inculcates both the good things: momentum and the adaptive learning rates
Adam = RMSProp + Momentum

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Adam = RMSProp + Momentum

- ② $m1 = 0$

$m2 = 0$

```
for i in range(max_iters):
```

```
→  $dw = \text{grad}(J, w, x, y)$ 
```

```
→  $m1 = \beta_1 \cdot m1 + (1 - \beta_1) \cdot dw$ 
```

```
→  $m2 = \beta_2 \cdot m2 + (1 - \beta_2) \cdot dw^2$ 
```

```
→  $w^- = \eta \cdot m1 / (\text{sqrt}(m2) + \epsilon)$ 
```

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- ② Bias correction is performed (since the estimates start from 0)

Adam

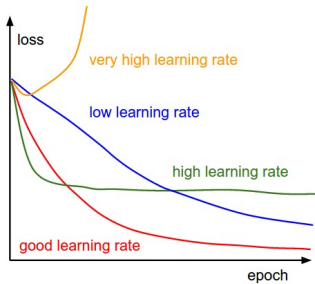


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→ $w- = \eta \cdot m1 / (\text{sqrt}(m2) + \epsilon)$
- ② Bias correction is performed (since the estimates start from 0)
- ③ Adam works well in practice (mostly with a fixed set of values for the hyper-params)



Learning rate scheduling

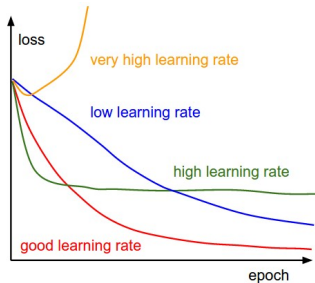
Learning rate (lr)



- What lr to use?

Figure credits: [CS231n-Stanford](#)

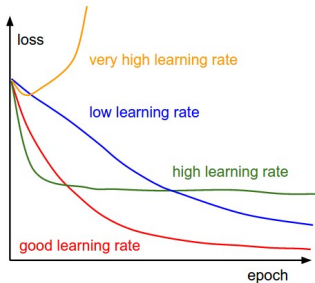
Learning rate (lr)



- What lr to use?
- Different lr at different stages of the training!

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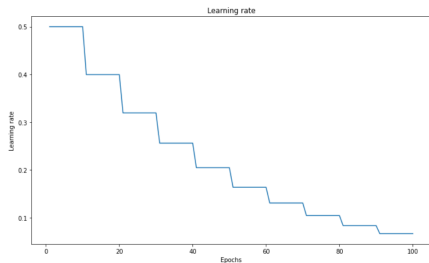
Learning rate (lr)



- What lr to use?
- Different lr at different stages of the training!
- Start with high lr and reduce it with time

Figure credits: [CS231n-Stanford](#)

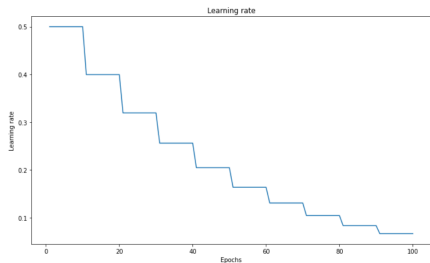
Learning Rate decay: Step



- 1 Reduce the lr after regular intervals

Figure credits: [Katherine Li](#)

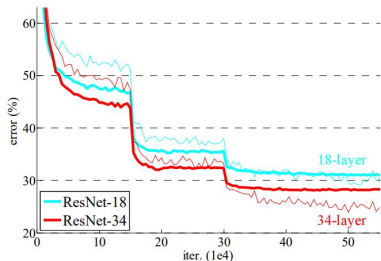
Learning Rate decay: Step



- 1 Reduce the lr after regular intervals
- 2 E.g. after every 30 epochs, $\eta^* = 0.1 \cdot \eta$

Figure credits: [Katherine Li](#)

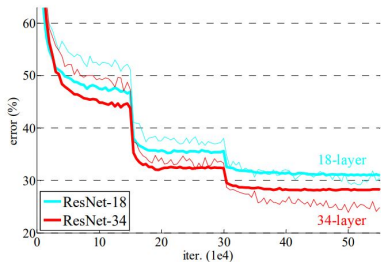
Learning Rate decay: Step



- ① Characteristic loss curve: different phases for 'stage'

Figure credits: Kaiming He et al. 2015, ResNets

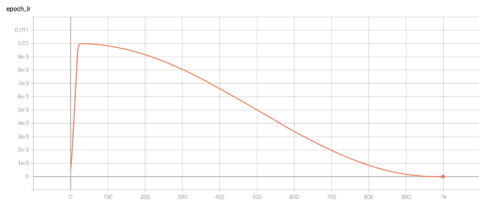
Learning Rate decay: Step



- ① Characteristic loss curve: different phases for 'stage'
- ② Issues: annoying hyper-params (when to reduce, by how much, etc.)

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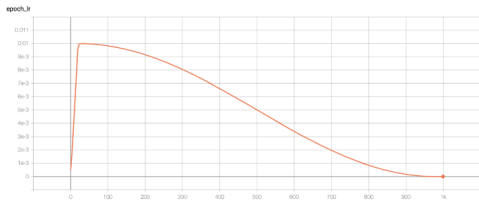
Learning Rate decay: Cosine



- 1 Reduces the lr continuously
$$\eta_t = \frac{1}{2}\eta_0(1 + \cos(t\pi/T))$$

Figure credits: [Sebastian Correa](#) and [Medium.com](#)

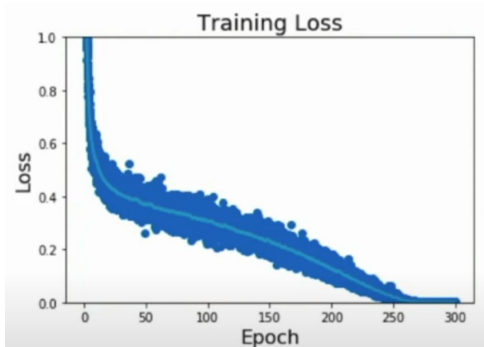
Learning Rate decay: Cosine



- 1 Reduces the lr continuously
$$\eta_t = \frac{1}{2}\eta_0(1 + \cos(t\pi/T))$$
- 2 Less number of hyper-parameters

Figure credits: [Sebastian Correa](#) and [Medium.com](#)

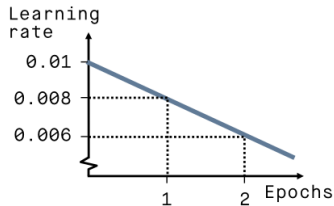
Learning Rate decay: Cosine



- ① Training longer tends to work, but initial lr is still a tricky one

Figure credits: Dr Justin Johnson, U Michigan

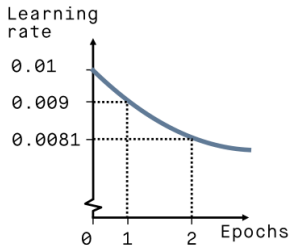
Learning Rate decay: Linear



$$\textcircled{1} \eta_t = \eta_0(1 - t/T)$$

Figure credits: peltarion.com

Learning Rate decay: Exponential



$$\textcircled{1} \eta_t = \eta_0 \cdot (1 - \alpha/100)^t$$

Figure credits: peltarion.com

Learning Rate decay: Constant lr



- ① No change in the learning rate

$$\eta_t = \eta_0$$



Learning Rate decay: Constant lr

- ① No change in the learning rate

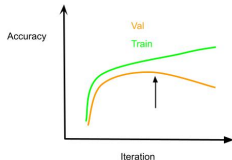
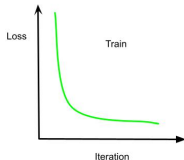
$$\eta_t = \eta_0$$

- ② Works for prototyping of ideas (other schedules may be better for squeezing in those 1-2% of gains in the performance)



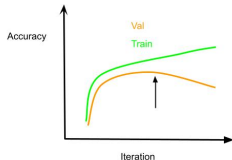
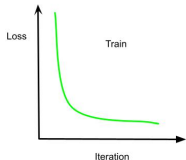
Early stopping - How many epochs to train?

Early stopping



- 1 Train as long as the validation performance improves (Stop when it deteriorates)

Early stopping



- ① Train as long as the validation performance improves (Stop when it deteriorates)
- ② Practice: train for a long number of epochs, saving the intermediate snapshots regularly, pick the one with the best val performance!

Good training practices



- Observe the initial loss value (if it is as expected or presence of bugs!)

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- Monitor the learning curves (tell us if poor initialization or over/under/right-fitting)

Good training practices



- Observe the initial loss value (if it is as expected or presence of bugs!)
- One may try to overfit to a very small subset to ensure the basic things are in place
- Monitor the learning curves (tell us if poor initialization or over/under/right-fitting)
- Use frameworks' (or fora) help for observing the learning dynamics (e.g. Tensorboard)



After the training

Model Ensembles



- Train multiple models independently and take average inference during testing

Model Ensembles



- Train multiple models independently and take average inference during testing
- Generally results in slight performance improvements

Model Ensembles



- The experts can be different snapshots of the same model from training

Model Ensembles



- The experts can be different snapshots of the same model from training
- E.g. trained with a periodic lr scheduling

Model Ensembles



- Moving average of parameters for testing (Polyak Averaging)
for i in range(max_iters):
 - $dw = \text{grad}(J, w, x, y)$
 - $w+ = -\eta \cdot dw$
 - $w_{\text{test}} = 0.95 \cdot w_{\text{test}} + 0.05 \cdot w$



Transfer Learning

Transfer learning: Pretrained features



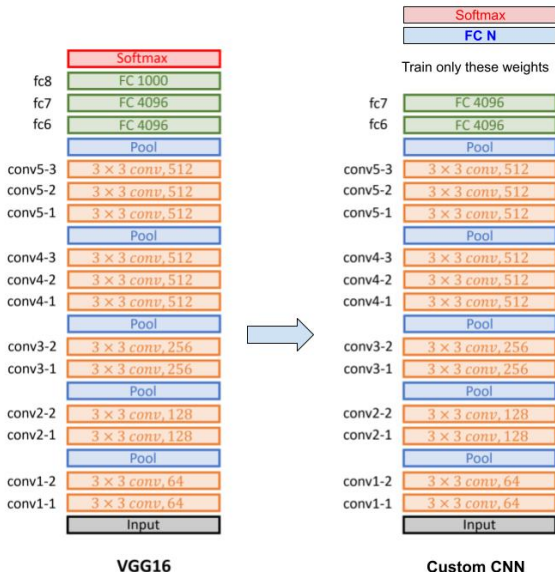
- Sometimes, we may get away with lesser training data!

Transfer learning: Pretrained features

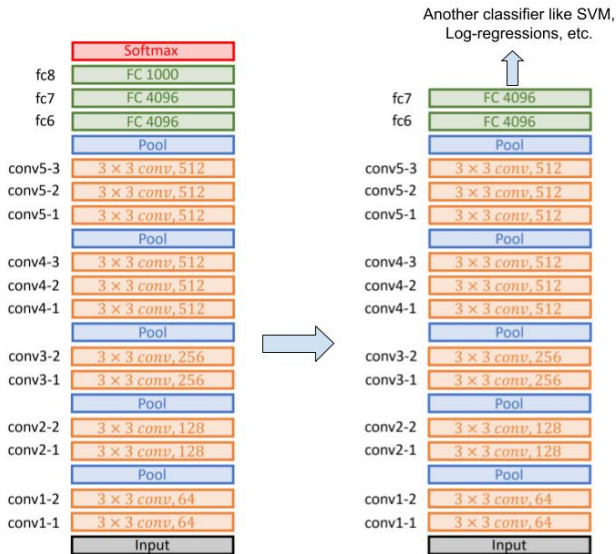


- Sometimes, we may get away with lesser training data!
- Take a DNN trained on a huge training data (task), use it as a feature extractor!!

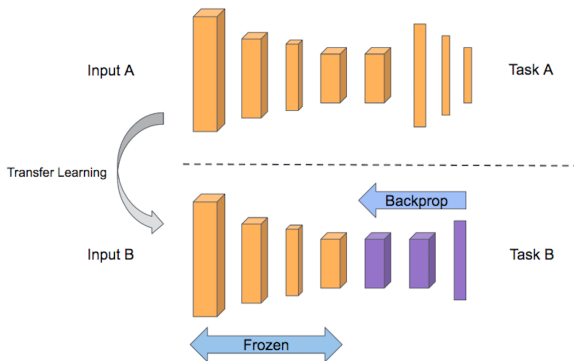
Transfer learning: Pretrained features



Transfer learning: Pretrained features



Transfer learning: Pretrained features and Finetuning



Some tips: may have to use smaller learning rate for the transferred layers, start with feature extraction then do finetuning, lower layers might be frozen, etc.

Figure credits: [Giang Tran and Medium.com](#)



Appendix

Convex function

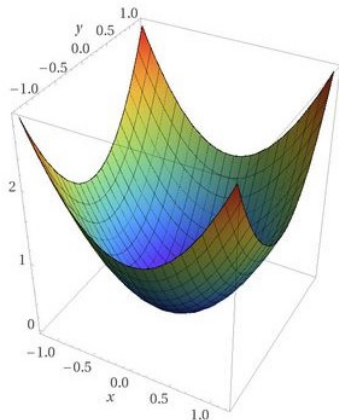


Figure credits: Paperspace blog

Level sets and ravine

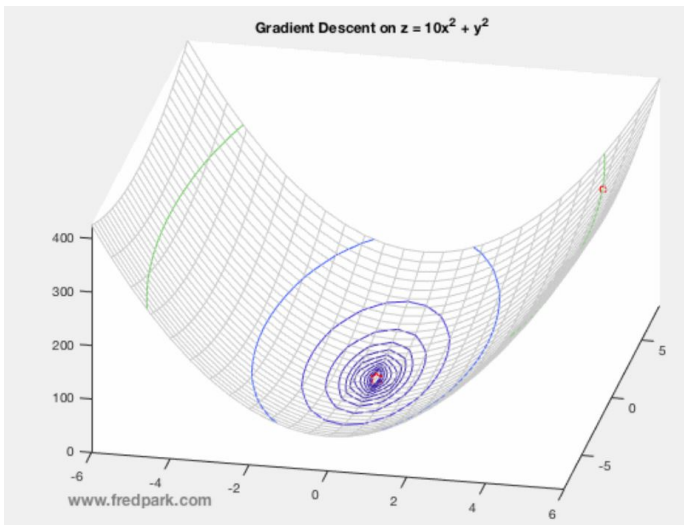


Figure credits: fredpark.com