

# **Deep Learning**

#### 12. Recurrent Neural Networks

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#### Perceptron, MLP, Gradient Descent (Backpropagation)



Perceptron, MLP, Gradient Descent (Backpropagation)CNNs



- Perceptron, MLP, Gradient Descent (Backpropagation)
- ② CNNs
- ③ 'Feedforward Neural networks'

#### Feedforward NNs: some observations



Size of the i/p is fixed(?!)

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- ② Successive i/p are i.i.d.

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- Size of the i/p is fixed(?!)
- ② Successive i/p are i.i.d.
- 3 Processing of successive i/p is independent of each other



Q deep

G deep — Search with Google

- ( kuldeep birdar
- Q deepika padukone
- Q deepthi sunaina
- Q deepak bagga
- Q deepika pilli
- Q deepti sharma

 Successive i/p are not independent



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- 3 Same underlying task at different 'time instances'



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- ② Length of the i/p is not fixed (→ predictions also)
- 3 Same underlying task at different 'time instances'
- ④ Sequence Learning Problems





#### Sentiment Analysis (Source)





POS-Tagging (Source:Kaggle)





Action Recognition (Source)





Image Captioning(Source)





#### Source

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one to many

Source





Source





Source



Source

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भारतीय प्राँद्योगिकी संस्थान हैवरावाद Indian Institute of Technology Hyderabad

# Can we not use the tools we already know to the tools we are already

• How about convolution?



INNs designed to solve sequence learning tasks



- INNs designed to solve sequence learning tasks
- ② Characteristics
  - $\textcircled{\ } \textbf{ 0 } \quad \text{Model the dependence among the } i/p$



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- INNs designed to solve sequence learning tasks
- ② Characteristics
  - $\textcircled{1} \quad \textbf{Model the dependence among the } i/p$
  - 2 Handle variable length of i/p
  - 3 Same function applied at all time instances
- They are Non-linear Auto-regressive Models

#### **RNNs:** internal state





#### **RNNs: unfolding**









(1) Apply the same transformation at every time step  $\rightarrow$  'Recurrent' NNs





**①** Apply the same transformation at every time step  $\rightarrow$  'Recurrent' NNs **②** i/p sequence  $x_t \in \mathbb{R}^{\mathbb{D}}$ 

#### **RNNs**



- (1) Apply the same transformation at every time step  $\rightarrow$  'Recurrent' NNs
- **2** i/p sequence  $x_t \in \mathbb{R}^{\mathbb{D}}$
- (3) Initial recurrent state  $h_0 \in \mathbb{R}^{\mathbb{Q}}$

#### **RNNs**



- (1) Apply the same transformation at every time step  $\rightarrow$  'Recurrent' NNs
- **2** i/p sequence  $x_t \in \mathbb{R}^{\mathbb{D}}$
- 3 Initial recurrent state  $h_0 \in \mathbb{R}^Q$
- ③ RNN model computes sequence of recurrent states iteratively  $h_t = \phi(x_t, h_{t-1}; w)$

#### **RNNs**





## Elmon RNN (1990)



(1) Start with  $h_0 = 0$ 

# Elmon RNN (1990)



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Use the same set of parameters at each time step





1 Use the same set of parameters at each time step





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- कुरुठेवेळा अन्वर्डेवेड क्रिइठ केव्यु केव केव्यु केव्यु
- 1 Use the same set of parameters at each time step
- ② Flexible to realize different variants (with some tricks!)



#### **Multi-layered RNNs**



1 Stack multiple RNNs between i/p and o/p layers



Source

#### **Multi-layered RNNs**



**1** Stack multiple RNNs between i/p and o/p layers

2 
$$H_t^{(l)} = W_{xh}^{(l)} \cdot H_t^{(l-1)} + W_{hh}^{(l)} \cdot H_{t-1}^{(l)} + b_h^{(l)}$$



Source

Consider a many-to-one variant RNN (e.g. sentiment analysis)



#### Backpropagation Through Time (BPT) worker detailed even a formation

- Consider a many-to-one variant RNN (e.g. sentiment analysis)
- 2 Let's separate the parameters into U, V, and W



Let's now perform SGD (assume loss L is formulated on y<sub>p</sub>)



## Backpropagation Through Time (BPT) webbe decide dec

- Let's now perform SGD (assume loss L is formulated on y<sub>p</sub>)



$$\begin{array}{ll} \textcircled{1} & \frac{\partial L}{\partial V} = \frac{\partial L}{\partial y_p} \frac{\partial y_p}{\partial V} = \\ & \frac{\partial L}{\partial y_p} \cdot \frac{\partial y_p}{\partial z_3} \cdot \frac{\partial z_3}{\partial V} \end{array}$$





$$\begin{array}{lll} \begin{tabular}{ll} \hline $\partial L$ & = $\partial L$ & $\partial y_p$ & $\partial y_p$ \\ \hline $\partial V$ & = $\partial y_p$ & $\partial y_p$ & $\partial z_3$ \\ \hline $\partial y_p$ & $\partial y_p$ & $\partial z_3$ & $\partial V$ \\ \hline $2$ & $y_p$ = $softmax(z_3)$ and $z_3$ = $V$ $\cdot$ $h_3$ + $b_y$ \\ \end{array}$$

3 Since we know that  $h_3, b_y$  are independent of V, we can compute  $\frac{\partial L}{\partial V}$  in a single step



1 Let's now consider  $\frac{\partial L}{\partial W}$ 



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#### Backpropagation Through Time (BPT) worker detailed even a formation

- 1 Let's now consider  $\frac{\partial L}{\partial W}$
- There are multiple 'W's in the computational graph!





 For ease of understanding



 $\begin{array}{c} \textcircled{1} \quad \underline{\Delta w} \text{ change in } \mathbb{W} \\ \\ \left( \frac{\partial h_1}{\partial W} \cdot \Delta w \right) \text{ change in } h_1 \end{array}$ 



- $\begin{array}{c} \textcircled{0} \quad \underline{\Delta w} \text{ change in } \mathbb{W} \\ \\ \left( \frac{\partial h_1}{\partial W} \cdot \Delta w \right) \text{ change in } h_1 \end{array}$



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- $\begin{array}{l} \textbf{3} \quad \Delta w \text{ change in } \mathsf{W} \rightarrow \\ \left( \frac{\partial h_3}{\partial W} \cdot \Delta w \right) \text{ change in } h_3 \end{array}$











$$\begin{aligned} & \Delta L = \\ & \frac{\partial L}{\partial h_1} \cdot \Delta h_1 + \frac{\partial L}{\partial h_2} \cdot \Delta h_2 + \frac{\partial L}{\partial h_3} \cdot \Delta h_3 \\ & 2 \quad \frac{\partial L}{\partial W} = \frac{\partial L}{\partial h_1} \frac{\partial h_1}{\partial W} + \frac{\partial L}{\partial h_2} \frac{\partial h_2}{\partial W} + \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial W} \\ & 3 \quad \frac{\partial L}{\partial h_3} = \frac{\partial L}{\partial y_p} \frac{\partial y_p}{\partial h_3} \end{aligned}$$



$$\begin{aligned} \Delta L &= \\ \frac{\partial L}{\partial h_1} \cdot \Delta h_1 + \frac{\partial L}{\partial h_2} \cdot \Delta h_2 + \frac{\partial L}{\partial h_3} \cdot \Delta h_3 \\ \end{aligned} \\ \begin{aligned} \partial \frac{\partial L}{\partial W} &= \frac{\partial L}{\partial h_1} \frac{\partial h_1}{\partial W} + \frac{\partial L}{\partial h_2} \frac{\partial h_2}{\partial W} + \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial W} \\ \end{aligned} \\ \end{aligned} \\ \begin{aligned} \partial \frac{\partial L}{\partial h_3} &= \frac{\partial L}{\partial y_p} \frac{\partial y_p}{\partial h_3} \\ \end{aligned} \\ \end{aligned} \\ \end{aligned} \\ \begin{aligned} \partial \frac{\partial L}{\partial h_2} &= ? \end{aligned}$$



$$\begin{array}{l} \mathbf{\Delta} L = \\ \frac{\partial L}{\partial h_1} \cdot \Delta h_1 + \frac{\partial L}{\partial h_2} \cdot \Delta h_2 + \frac{\partial L}{\partial h_3} \cdot \Delta h_3 \\ \mathbf{2} \quad \frac{\partial L}{\partial W} = \frac{\partial L}{\partial h_1} \frac{\partial h_1}{\partial W} + \frac{\partial L}{\partial h_2} \frac{\partial h_2}{\partial W} + \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial W} \\ \mathbf{3} \quad \frac{\partial L}{\partial h_3} = \frac{\partial L}{\partial y_p} \frac{\partial y_p}{\partial h_3} \\ \mathbf{4} \quad \frac{\partial L}{\partial h_2} = ? \\ \mathbf{5} \quad \frac{\partial L}{\partial h_2} = \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial h_2} \end{array}$$



## Backpropagation Through Time (BPT) website defined where a stream

$$\begin{array}{ll} \mathbf{\Delta} L = \\ \frac{\partial L}{\partial h_1} \cdot \Delta h_1 + \frac{\partial L}{\partial h_2} \cdot \Delta h_2 + \frac{\partial L}{\partial h_3} \cdot \Delta h_3 \\ \mathbf{2} \quad \frac{\partial L}{\partial W} = \frac{\partial L}{\partial h_1} \frac{\partial h_1}{\partial W} + \frac{\partial L}{\partial h_2} \frac{\partial h_2}{\partial W} + \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial W} \\ \mathbf{3} \quad \frac{\partial L}{\partial h_3} = \frac{\partial L}{\partial y_p} \frac{\partial y_p}{\partial h_3} \\ \mathbf{4} \quad \frac{\partial L}{\partial h_2} = ? \\ \mathbf{5} \quad \frac{\partial L}{\partial h_2} = \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial h_2} \\ \mathbf{6} \quad \frac{\partial L}{\partial h_1} = \frac{\partial L}{\partial h_2} \frac{\partial h_3}{\partial h_1} = \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial h_2} \frac{\partial h_2}{\partial h_1} \end{aligned}$$



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$$\frac{\partial L}{\partial W} = \sum_{k=1}^{3} \frac{\partial L}{\partial h_3} \frac{\partial h_3}{\partial h_k} \frac{\partial h_k}{\partial W}$$



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 Consider a many-to-many variant RNN (e.g. PoS tagging)



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- Full sequence is one training example (although there is an error computed at each time step)



- Consider a many-to-many variant RNN (e.g. PoS tagging)
- 2 Total error is the sum of errors at each time step



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 $\frac{\partial L}{\partial W} = \sum_{k=1}^{3} \frac{\partial L}{\partial h_3} \left( \prod_{j=k+1}^{3} \frac{\partial h_j}{\partial h_{j-1}} \right) \frac{\partial h_k}{\partial W}$ 

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Leads to Vanishing Gradient problem!

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- 4 Leads to Vanishing Gradient problem!
- So impact of earlier time steps at later times (difficult to learn long-term dependencies!)

3

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  - Gradient clipping

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- Better initialization, Regularization, short time sequences (Truncation)

## Backpropagation Through Time (BPT) works dated and a log bound works of the second and the secon



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#### Handling long-term dependencies



Architectural modifications to RNNs

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#### Architectural modifications to RNNs

• LSTM (1997 by Sepp Hochreiter and Jürgen Schmidhuber; Improved by Gers et al. in 2000)

#### Handling long-term dependencies



#### Architectural modifications to RNNs

- LSTM (1997 by Sepp Hochreiter and Jürgen Schmidhuber; Improved by Gers et al. in 2000)
- GRU (Cho et al. 2014)





Long Short-Term Memory





- Long Short-Term Memory
- 2 At a time 't', hidden state  $h^{(t)}$  and cell state  $c^{(t)}$





- Long Short-Term Memory
- ② At a time 't', hidden state  $h^{(t)}$  and cell state  $c^{(t)}$ 
  - Cell stores long-term information



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- 3 What to erase/write/read is controltted by corresponding gates
  - At time t, elements of the gates can be 0 (closed), 1 (open), or in-between
  - Gates are dynamically computed based on the context





RNNs are chain of repeating moduels. Basic RNN (Colah's blog)





RNNs are chain of repeating moduels. LSTM (Colah's blog)





The LSTM node. (Colah's blog)

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#### LSTM: The cell state





#### LSTM: The cell state

 Info. can flow through unchanged







- Info. can flow through unchanged
- ② Gates can add/remove information to cell state



#### LSTM: The gates



Sigmoid neural nets (o/p numbers in [0, 1])



### LSTM: The gates





- Sigmoid neural nets (o/p numbers in [0, 1])
- 2 Point-wise multiplication operation

#### LSTM: The forget gate



 Decides what to throw away from cell state (e.g. forgetting the gender of old subject in light of a new one)



$$f_t = \sigma \left( W_f \cdot [h_{t-1}, x_t] + b_f \right)$$

Forget gate in LSTM (Colah's blog)

### LSTM: The input gate



Next is to decide what new to store in cell state (e.g. add the gender of a new subject)





Input gate in LSTM (Colah's blog)

### LSTM: The input gate

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- Next is to decide what new to store in cell state (e.g. add the gender of a new subject)
- 2 Done in two steps
  - input gate decides what to update
  - A tanh layer creates a candidate cell state



$$\begin{split} i_t &= \sigma \left( W_i {\cdot} [h_{t-1}, x_t] \ + \ b_i \right) \\ \tilde{C}_t &= \tanh(W_C {\cdot} [h_{t-1}, x_t] \ + \ b_C) \end{split}$$

Input gate in LSTM (Colah's blog)

#### LSTM: The cell state update





#### LSTM: The output





$$o_t = \sigma \left( W_o \left[ h_{t-1}, x_t \right] + b_o \right)$$
$$h_t = o_t * \tanh \left( C_t \right)$$

Output computation in LSTM (Colah's blog)

e.g. may be a verb that is coming next in case of a language model

#### LSTM variant: Peephole connections



$$\begin{split} f_{t} &= \sigma \left( W_{f} \cdot [\boldsymbol{C_{t-1}}, h_{t-1}, x_{t}] + b_{f} \right) \\ i_{t} &= \sigma \left( W_{i} \cdot [\boldsymbol{C_{t-1}}, h_{t-1}, x_{t}] + b_{i} \right) \\ o_{t} &= \sigma \left( W_{o} \cdot [\boldsymbol{C_{t}}, h_{t-1}, x_{t}] + b_{o} \right) \end{split}$$

Variant with gates looking into the Cell state in LSTM by Ger et al. (Colah's blog)

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### LSTM variant: Coupled i/p and forget gates



 $C_t = f_t * C_{t-1} + (1 - f_t) * \tilde{C}_t$ 

Variant with coupled input and forget gates. (Colah's blog)

#### $\textbf{LSTM} \rightarrow \textbf{GRU}$





$$z_t = \sigma \left( W_z \cdot [h_{t-1}, x_t] \right)$$
  

$$r_t = \sigma \left( W_r \cdot [h_{t-1}, x_t] \right)$$
  

$$\tilde{h}_t = \tanh \left( W \cdot [r_t * h_{t-1}, x_t] \right)$$
  

$$h_t = (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t$$

Gated Recurrent Unit (Colah's blog)



I Via the gates!

# LSTM: handling the vanishing gradients



1 Computational graph at time k-1
#### భారతీయ పొంకేతిక విజ్ఞాన సంస్థ హైదరాబాద్ LSTM: handling the vanishing gradients भारतीय प्रांद्योगिर्ळ Indian Institute of Techn



 $tanh(W_c[h_{t-1}, x_t] + b_c)$ 

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#### All the gates

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# LSTM: handling the vanishing gradients web added to the second added the second added to the second added



#### Next hidden state



Running till time step 't'



 Consider loss computation

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Let's know if the 1 gradient flows to an arbitrary time step 'k'

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## LSTM: handling the vanishing gradients under dative dative



 Specifically, let's consider if gradient flows to W<sub>f</sub> through C<sub>k</sub>



- Specifically, let's consider if gradient flows to W<sub>f</sub> through C<sub>k</sub>
- Note that there are multiple paths between L and C<sub>k</sub> (but, consider one such path as highlighted)



 $\begin{array}{l} \bullet \quad \text{Grad} = \\ \frac{\partial L}{\partial h_t} \frac{\partial h_t}{\partial C_t} \frac{\partial C_t}{\partial C_{t-1}} \cdots \frac{\partial C_{k+1}}{\partial C_k} \end{array}$ 



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- 2  $\frac{\partial L}{\partial h_t}$  doesn't vanish (no intermediate nodes)



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# LSTM: handling the vanishing gradients under dative dative



$$C_t = f_t \odot C_{t-1} + i_t \odot \tilde{C}_t$$



- $C_t = f_t \odot C_{t-1} + i_t \odot \tilde{C}_t$
- Note that C
  t
  t
  depends on
  C
  t
  -1, and for simplicity
  assume the gradient
  from that term vanishes



- $C_t = f_t \odot C_{t-1} + i_t \odot \tilde{C}_t$
- Note that *C<sub>t</sub>* depends on *C<sub>t-1</sub>*, and for simplicity assume the gradient from that term vanishes

3 Grad =  

$$\frac{\partial L}{\partial h_t} \frac{\partial h_t}{\partial C_t} \frac{\partial C_t}{\partial C_{t-1}} \cdots \frac{\partial C_{k+1}}{\partial C_k}$$



- $C_t = f_t \odot C_{t-1} + i_t \odot \tilde{C}_t$
- Note that *C<sub>t</sub>* depends on *C<sub>t-1</sub>*, and for simplicity assume the gradient from that term vanishes
- $\begin{array}{l} \textbf{3} \quad \textbf{Grad} = \\ \frac{\partial L}{\partial h_t} \frac{\partial h_t}{\partial C_t} \frac{\partial C_t}{\partial C_{t-1}} \cdots \frac{\partial C_{k+1}}{\partial C_k} \end{array}$



#### 



- 2 Red term vanishes only if during the forward pass this product caused the information to vanish (by the time 't')!

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- 3 That means, gradient will vanish only if dependency in the forward pass vanishes! (which makes sense)
- ④ Gates do the same regulation in backward pass as they do in the forward





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- 3 Attention and Transformers are becoming more popular lately